

Advanced Exergy Analysis of Gas Turbines

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Introductory Concepts

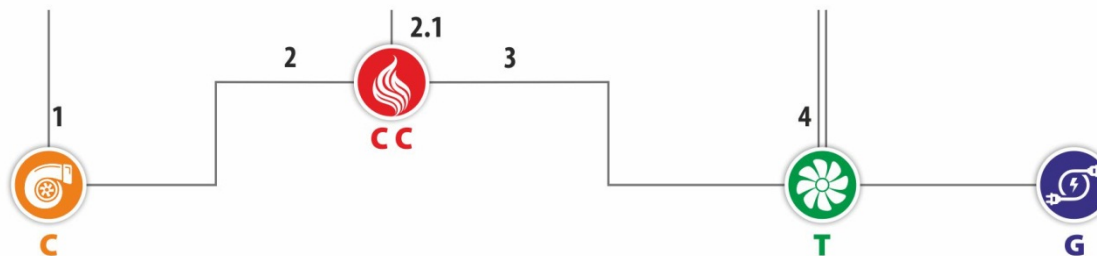
- **1st** Thermodynamic Law – **energy** analysis
- **2nd** Thermodynamic Law – **exergy** analysis

based on

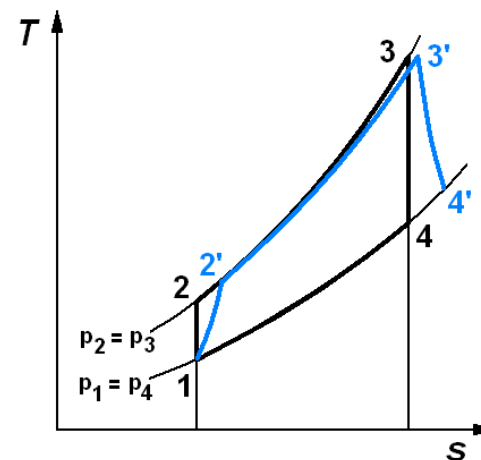
Entropy **Generation** → Exergy **Destruction**

$$I = T_0 S_{gen} \geq 0$$

Single-shaft Power Gas Turbine (GT)



- 1: Compressor
- 2-3: Combustion Chamber
- 4: Turbine



Performance of GT- Energy Analysis

p_0 (bar)
 T_0 (oC)
 K_{in} (%)
 π_c
 $\eta_{is,c}$ (%)
 η_b (%)
 q_f (kJ/kg)
 K_b
 T_{t4} (oC)
 $\eta_{is,t}$ (%)
 K_{ex} (%)
 γ_a
 c_{pa} (J/kg/K)
 γ_g
 c_{pg} (J/kg/K)
 η_m
 ea
 eg
 ma (kg/s)

Physics equations



pt_1
 T_{t1}
 pt_2
 T_{t2}
 pt_3
 T_{t3}
 pt_4
 T_{t4}
 pt_5
 T_{t5}
 pt_6
 T_{t6}

1st Thermodynamic Law



w_c
 w_t
 w_k
 η_θ
 sfc

Exergy Analysis-Kinds of Exergy

- Thermal Exergy

$$E^T = C_p^h (T - T_0 - T_0 \ln \frac{T}{T_0}) \text{ (J/kg)}$$

- Mechanical Exergy

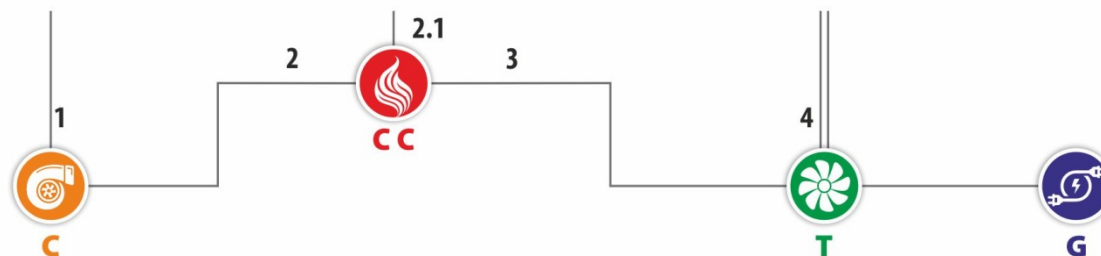
$$E^M = RT_0 \ln \frac{p}{p_0} \text{ (J/kg)}$$

- Chemical Exergy

$$E^{CHE} = \frac{\varepsilon^{\sim 0, M}}{M B_{fuel}} \text{ (J/kg)}$$

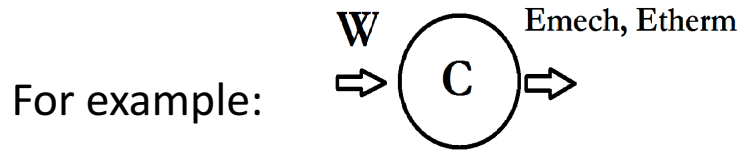
CEA Results 1/3

	State	Mass flow (kg/sec)	Pressure (bar)	Temperature (K)	E^T (kW)	E^M (kW)	E^{CHE} (kW)
Air in C	1	1,00	0,995	273	0,000	-1,172	0,000
Air in CC	2	1,00	13,057	643,8	137,272	200,530	0,000
Fuel in CC	2.1	0,023	2	298	0,042	0,,613	1115,54
Gas in T	3	1,023	12,405	1373	690,366	198,934	0,000
Exhaust Gases	4	1,023	1,031	822,8	260,437	1,632	0,000



CEA Results 2/3

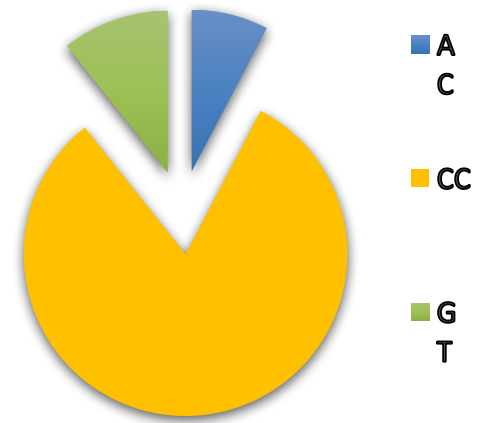
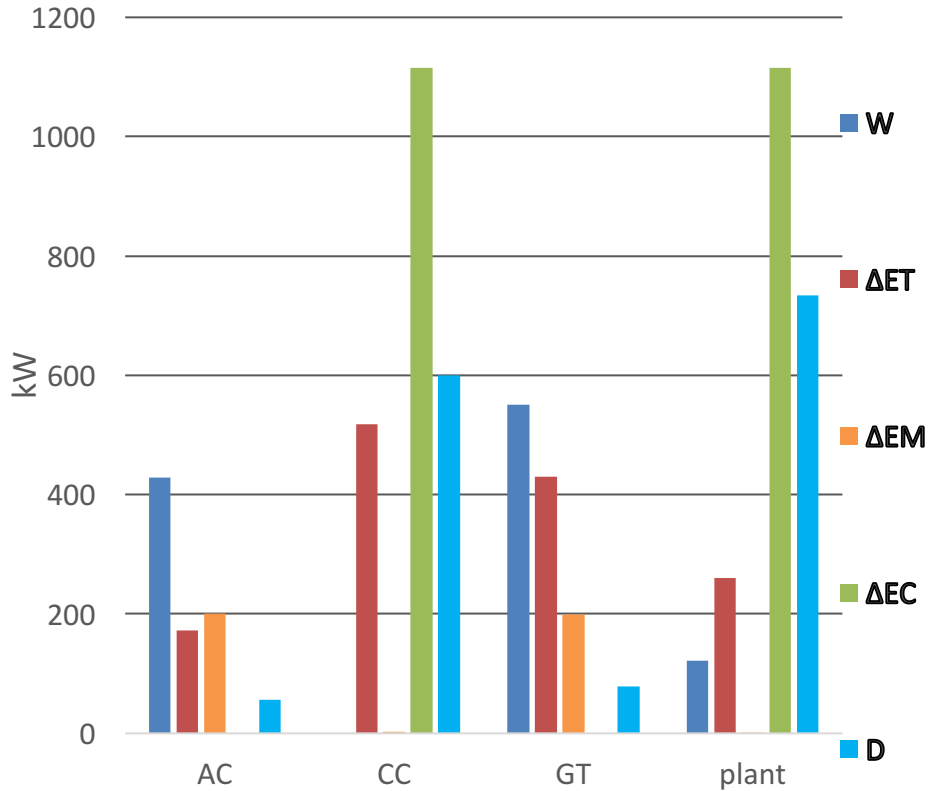
Exergy Balance: $E_{F,k} = E_{P,k} + I_k$



Also, we define ϵ as: $\frac{E_{P,k}}{E_{F,k}}$

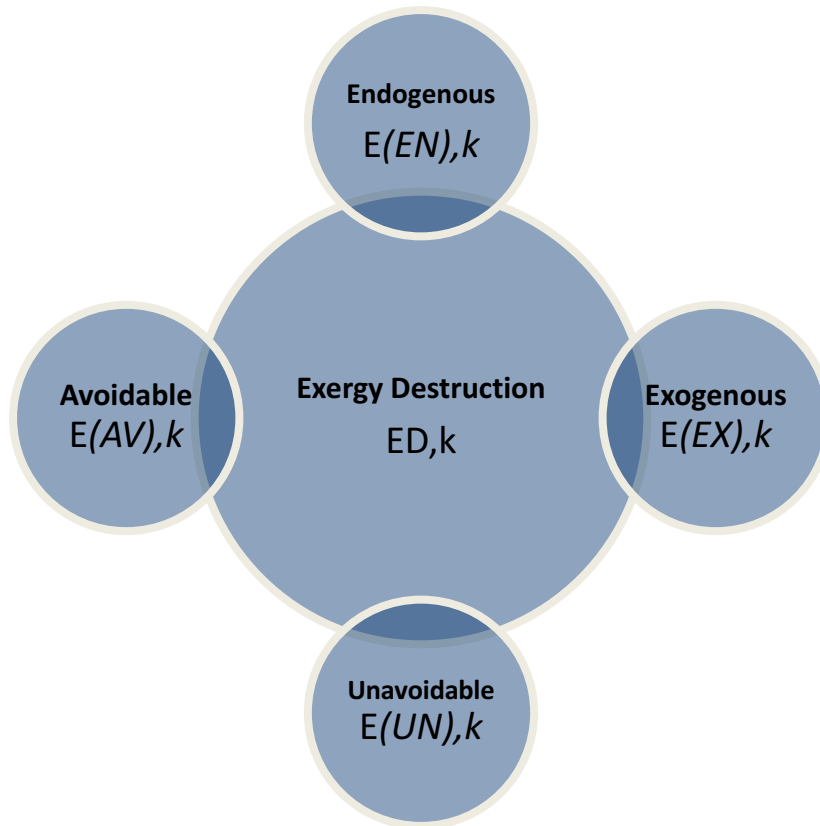
	$E_{F,k}$ (kW)	$E_{P,k}$ (kW)	$E_{D,k} = I_k$ (kW)	ϵ (-)	ϵ %
C	372,654	336,629	36,025	0,9033	90,33
CC	1115,54	550,844	564,696	0,4938	49,38
T	627,231	576,363	50,868	0,9189	91,89
Plant	1115,54	463,951	651,589	0,4159	41,59

CEA Results 3/3



Advanced Exergy Analysis (AEA)

Introductory Concepts



Endogenous: irreversibilities occurring within the component operating with its **real** efficiency

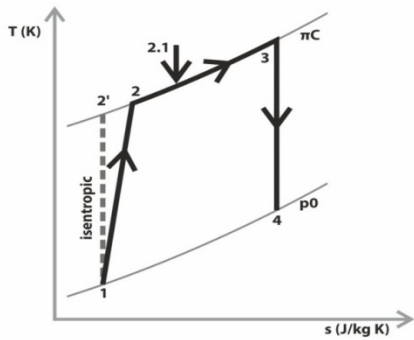
Exogenous: irreversibilities occurring within the other components operating with their **ideal** efficiency

Unavoidable: the part within the component, which cannot be reduced due to **thermodynamic limitations**

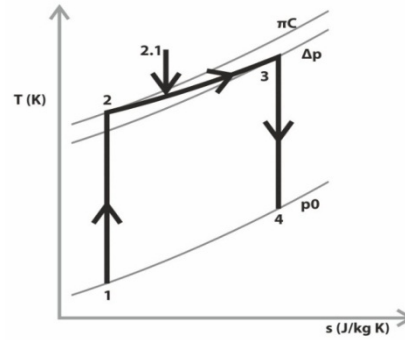
Avoidable: the part within the component, which **can be reduced** if the best available technology is applied.

AEA Methodology 1/4

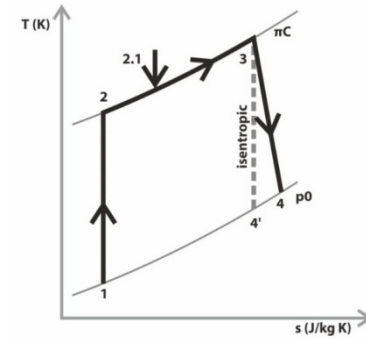
Endogenous Exergy Destruction → Hybrid Cycles



Hybrid Cycle C



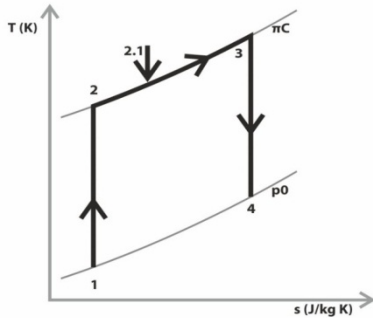
Hybrid Cycle CC



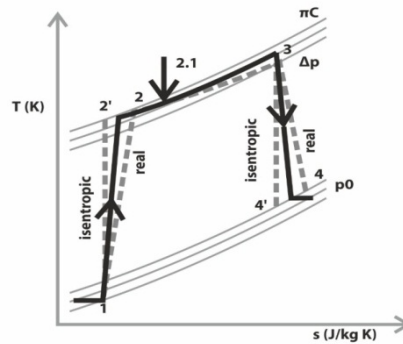
Hybrid Cycle T

AEA Methodology 2/4

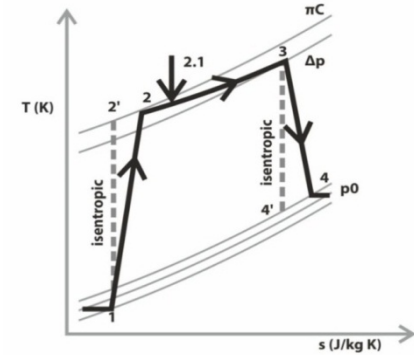
Unavoidable Exergy Destruction \rightarrow Unavoidable Cycle



Ideal Cycle



Unavoidable Cycle



Real Cycle

a (IDEAL) > **a** (UNAVOIDABLE) > **a** (REAL)

a could be replaced with: $\eta_{is,T}, \eta_{is,C}, \eta_b, \Delta p, K_{IN}, K_{OUT}$

AEA Methodology 3/4

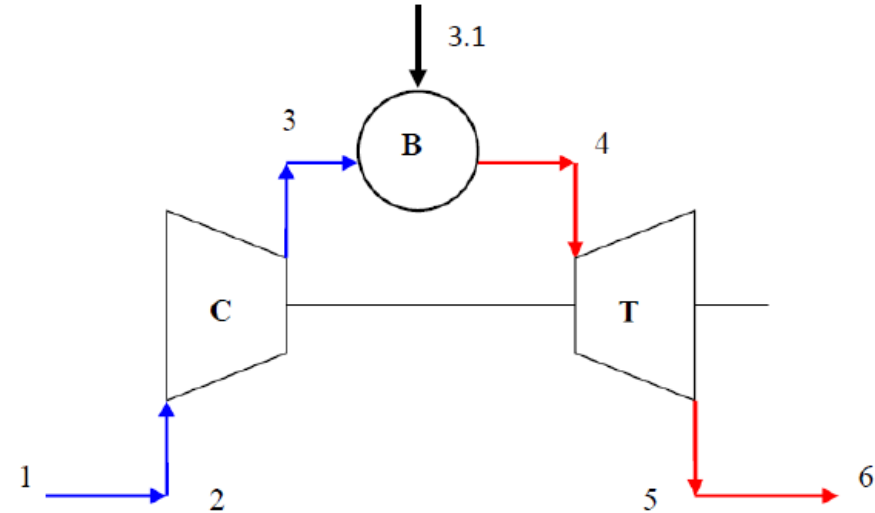
Constant in all cycles

- Gas Turbine Inlet Temperature (T_{t4})
- Engine Net power (W)
- Air-fuel ratio (λ)

Real cycle (RE)

$$m_3 + m_{3.1} = m_4$$

$$E_3 + \epsilon_{CC, \text{real}} E_{3.1} = E_4 \quad \mu \epsilon \quad \epsilon_{CC, \text{real}} \neq 1$$



Compressor's and Turbine's Hybrid Cycles (H.C, H.T) & Unavoidable cycle (UN)

$$m_3 + m_{3.1} \neq m_4,$$

$$E_3 + \epsilon_{CC} E_{3.1} = E_4, \text{ with } \epsilon_{CC} = 1 \text{ (hybrid C,T), } \epsilon_{CC} > \epsilon_{CC, \text{real}} \text{ (Unavoidable)}$$

Combustion Chamber's Hybrid Cycle (H.CC)

$$m_3 + m_{3.1} \neq m_4$$

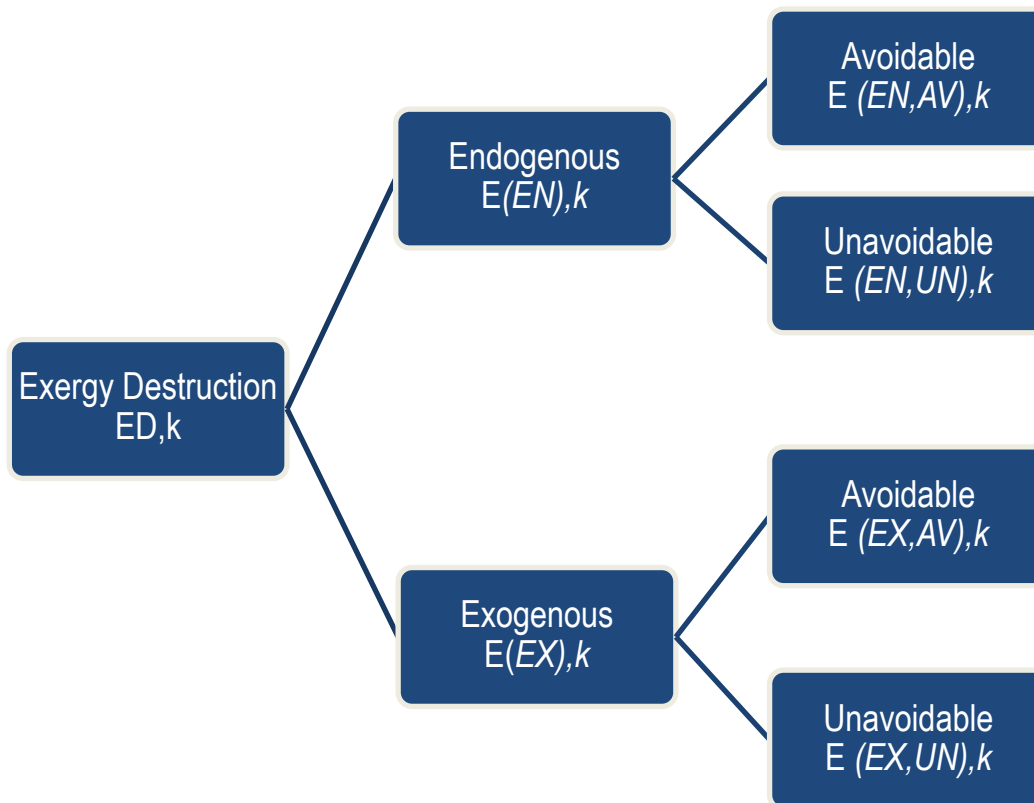
$$E_3 + \epsilon_{CC} E_{3.1} = E_4, \quad \mu \epsilon \quad \epsilon_{CC} = \epsilon_{CC, \text{real}}$$

$$m_3 e_3 + \epsilon_{CC} m_{3.1} e_{3.1} = m_4 e_4$$

$$W = \eta_{mm} W_T - m_3 W_C$$

$$m_3 = \lambda m_{3.1}$$

AEA Methodology 4/4



Example:

EN,AV : part of the exergy destruction within the component (**EN**), which can be reduced if the best available technology is applied (**AV**)

$$E(EN,AV),k + E(EX,AV),k + E(EX,UN),k + E(EN,UN),k = ED,k$$

AEA Results 1/2

Exergy Destruction E D,k		C	CC	T
<i>Endogenous</i>	E D,k (EN)	482.4	14233.3	1091.1
<i>Exogenous</i>	E D,k (EX)	682.4	4650.8	533.8
<i>Unavoidability Indicator</i>	Λ ,k	0.033	0.614	0.019
<i>Unavoidable</i>	E D,k (UN)	810.3	17971.8	798.6
<i>Avoidable</i>	E D,k (AV)	354.4	912.3	826.3
<i>Unavoidable-Endogenous</i>	E D,k (UN,EN)	360.6	13545.7	527.0
<i>Avoidable-Endogenous</i>	E D,k (AV,EN)	121.7	687.6	564.1
<i>Unavoidable-Exogenous</i>	E D,k (UN,EX)	449.7	4426.2	271.6
<i>Avoidable-Exogenous</i>	E D,k (AV,EX)	232.7	224.7	262.2

AEA Results 2/2

Compressor



- Endogenous Exergy D.
- Exogenous Exergy D.



- Unavoidable Exergy D.
- Avoidable Exergy D.



- Unavoidable Endogenous Exergy D.
- Avoidable Endogenous Exergy D.
- Unavoidable Exogenous Exergy D.
- Avoidable Exogenous Exergy D.

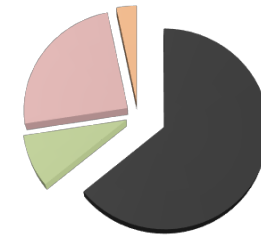
Combustion Chamber



- Endogenous Exergy D.
- Exogenous Exergy D.



- Unavoidable Exergy D.
- Avoidable Exergy D.



- Unavoidable Endogenous Exergy D.
- Avoidable Endogenous Exergy D.
- Unavoidable Exogenous Exergy D.
- Avoidable Exogenous Exergy D.

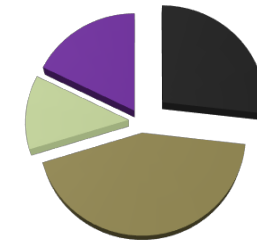
Turbine



- Endogenous Exergy D.
- Exogenous Exergy D.



- Unavoidable Exergy D.
- Avoidable Exergy D.



- Unavoidable Endogenous Exergy D.
- Avoidable Endogenous Exergy D.
- Unavoidable Exogenous Exergy D.
- Avoidable Exogenous Exergy D.

CONCLUSIONS

- The main Exergy Destruction is caused by **CC** (84,9%)
- Exogenous Exergy Destruction is lower than Endogenous in **CC, T**.
- Avoidable Exergy Destruction is greater than the Unavoidable part in **C, T**.
- Unavoidable Exergy Destruction is much greater than Avoidable Exergy Destruction in the **CC**
- On the contrary, **C, T** have their greater contribution in the Avoidable part

Future Research

- *AEA methodology in a whole power range of gas turbines to examine how it scales with power*
- *AEA methodology in further applications of gas turbine technology (recuperator, water injection)*
- *Extension AEA methodology, which could also include environmental and/or economical issues.*

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Thank you for your attention!

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